

```

def f(n):
    i = 1 + n
    return i + 2

```

```

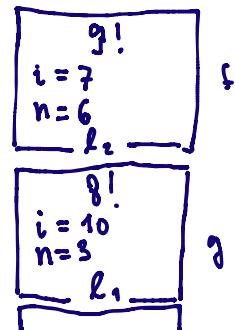
def g(n):
    i = 1 + f(n + 3)  $\ell_2$ 
    return i - 2

```

```

>>> g(3)  $\ell_1$ 
8

```



```

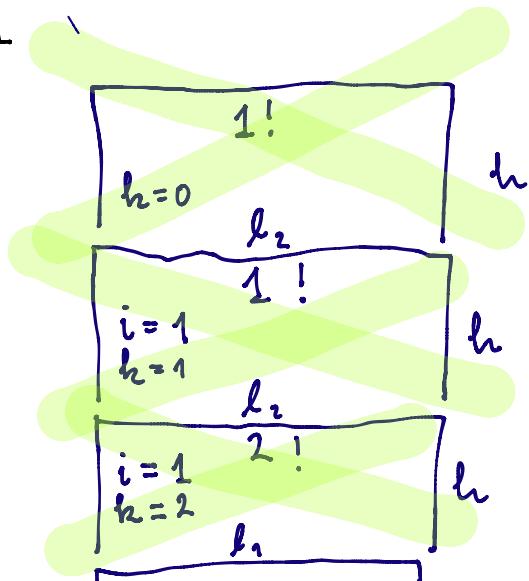
def h(k):
    if k == 0: return 1
    else:
        i = h(k-1)  $\ell_2$ 
        return k * i

```

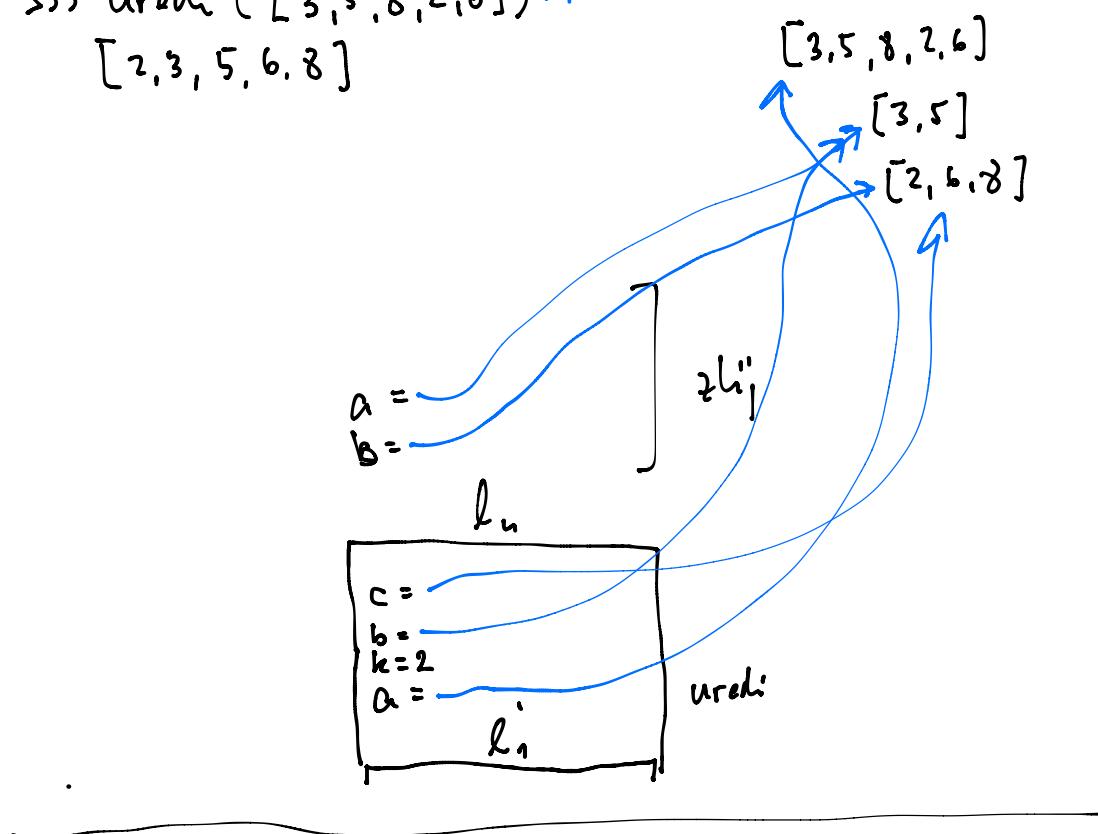
```

>>> h(2)  $\ell_1$ 
2

```



>>> uređi ([3,5,8,2,6])  
[2,3,5,6,8]



Časovna zahtevnost uređivanja &  
zlijenjem

$T(n) = \text{št. koraka za uređivanje}$   
tabele dulžine  $n$

$$T(0) = 1$$

$$T(1) = 1$$

$$T(n) = T(n/2) + T(n/2) + n$$

$$\begin{aligned}
 T(n) &= n + 2 \cdot T(n/2) \\
 &= n + 2 \cdot \left( \frac{n}{2} + 2 \cdot T\left(\frac{n}{4}\right) \right) \\
 &= n + n + 4 \cdot T\left(\frac{n}{4}\right) \\
 &= n + n + 4 \cdot \left( \frac{n}{4} + 2 \cdot T\left(\frac{n}{8}\right) \right) \\
 &= n + n + n + 8 \cdot T\left(\frac{n}{8}\right) \\
 &\quad \vdots \\
 &= \underbrace{n + n + \dots + n}_{k} + 2^k \cdot T\left(\frac{n}{2^k}\right) \\
 &\quad \swarrow \quad \text{?} \\
 &= (n \cdot \log_2 n) + 2^{\log_2 n} \cdot T(1) \quad \frac{n}{2^k} = 1 \\
 &= (n \cdot \log_2 n) + n \cdot 1 = n + n \cdot \log_2 n \\
 &= \underline{\underline{\mathcal{O}(n \cdot \log_2 n)}}
 \end{aligned}$$

$$T(n) = n + 3 \cdot T\left(\frac{n}{3}\right) \rightsquigarrow n \cdot \log n$$

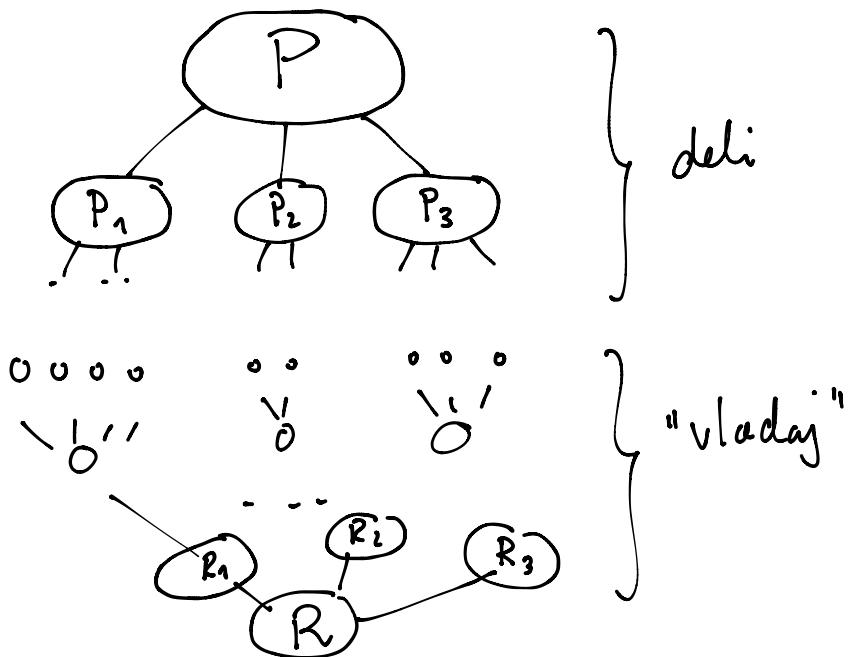
$$T(n) = n + 3 \cdot T\left(\frac{n}{4}\right) \rightsquigarrow ?$$

$$\text{?} \\ n + 3 \cdot T\left(\frac{n}{4}\right) =$$

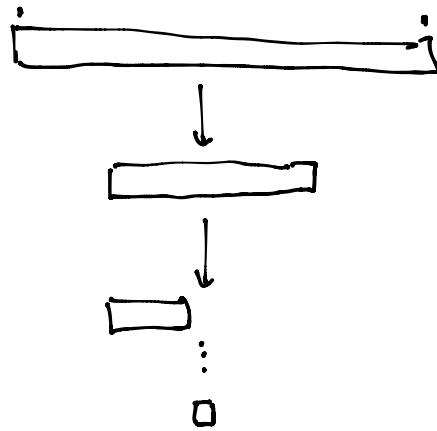
$$n + 3 \cdot \left( \frac{n}{4} + 3 \cdot T\left(\frac{n}{16}\right) \right) =$$

$$\begin{aligned}
 n + \frac{3}{4}n + 3^2 \cdot T\left(\frac{n}{4^2}\right) &= \\
 n + \frac{3}{4}n + \frac{3^2}{4^2}n + 3^3 T\left(\frac{n}{4^3}\right) &= \\
 n \cdot \left(1 + \frac{3}{4} + \left(\frac{3}{4}\right)^2 + \dots + \left(\frac{3}{4}\right)^k\right) + 3^{k+1} T\left(\frac{n}{4^{k+1}}\right) \\
 \leq n \cdot C &+ 3^{\log_4 n} \cdot 1 \\
 \leq C \cdot n + n^{\frac{\log_4 3}{\log_3 4}} & \\
 O(n) &
 \end{aligned}$$

DELI in VLADAJ

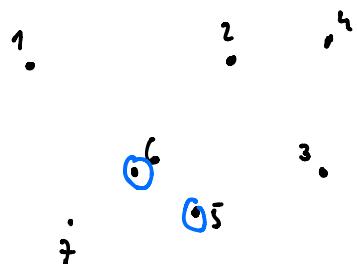


Primer: urejanje z zlivanjem  
bisekcija



Najbližji par točk

Naloga: imamo točke  $T_1, \dots, T_n$  v ravnini.  
Poisci par najbljžjih točk  $(T_i, T_j)$ .



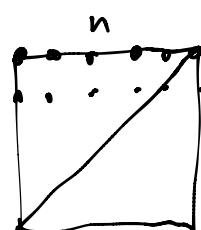
Preprosta rešitev:

Obravnavamo vse pary  $(T_i, T_j)$ ,  $i < j$

število parov:

$$\cancel{n^2 - n}$$
$$\frac{n^2 - n}{2}$$

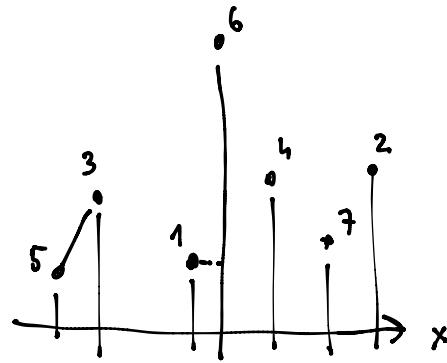
$\mathcal{O}(n^2)$



Izboljšamo:

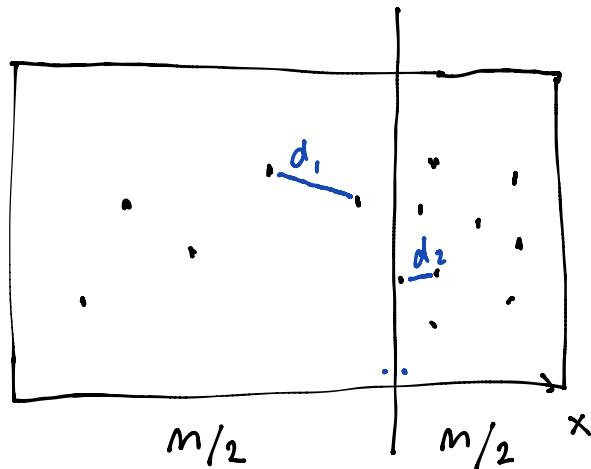
Ideja: "SORTIRAMO"

⋮  
⋮  
⋮  
⋮



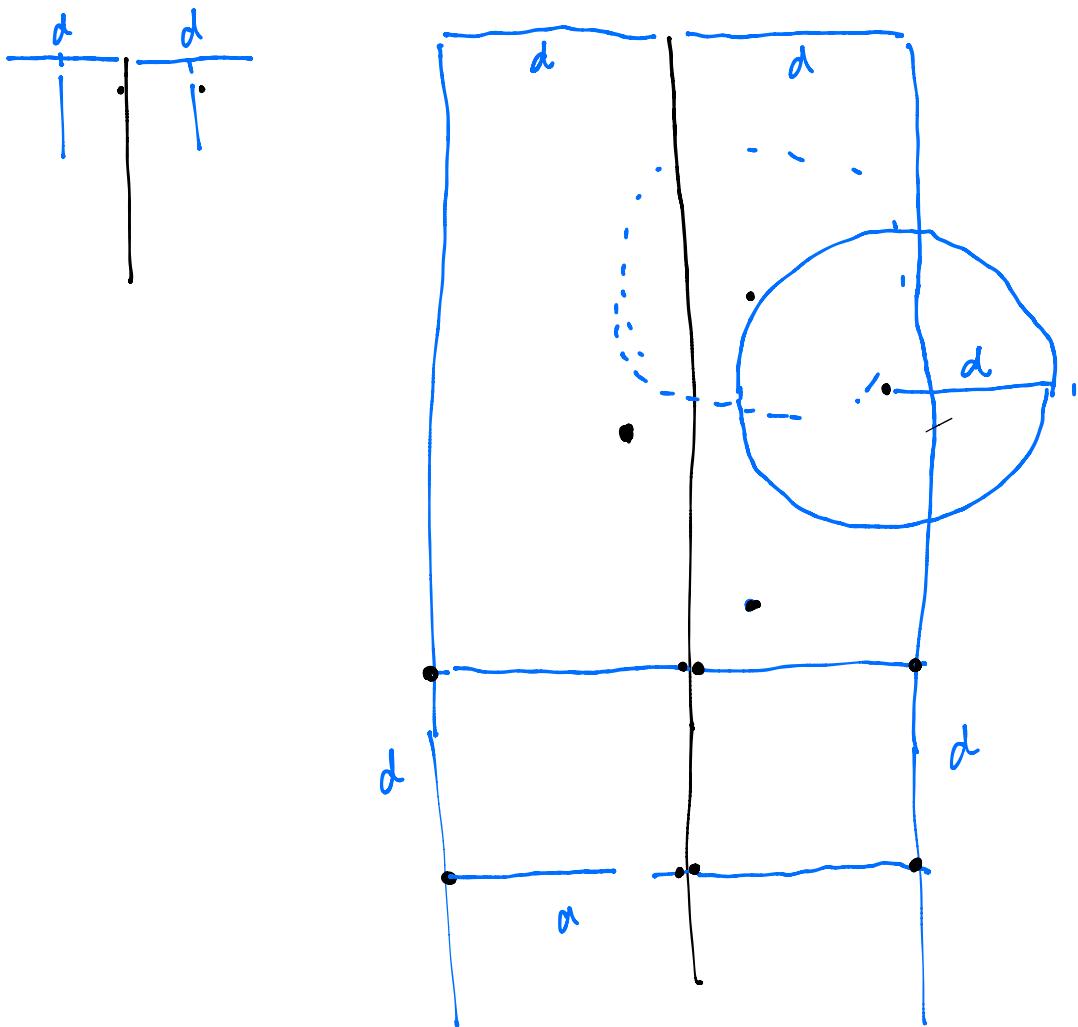
Ideja: "BISEKCIJA"

$$T(n) = 2 \cdot T\left(\frac{n}{2}\right) + \underline{\quad}$$



$$d = \min(d_1, d_2)$$

zlivanje: operujemo območje voki  
delilne črte širine  $2d$



najblížji par  $(T_1, \dots, T_n)$  :

if  $n \leq 2$ :

osnovni primer

$$(S, S', d_1) = \text{najblížji par } (T_1, \dots, T_{n/2})$$

$$(R, R', d_2) = \text{najblížji par } (T_{n/2+1}, \dots, T_n)$$

$$d = \min(d_1, d_2)$$

Obrannavaj pas jiné d okoli  
rzmijitene irte

Casova záleženosť  $T(n) = 2 \cdot T\left(\frac{n}{2}\right) + n$

$$\Theta(n \cdot \log n)$$